

PRACTICE PAPER TERM-I

CLASS-XII

SUB. : MATHEMATICS

TIME : 90 MIN.

MM: 40

General Instructions:

1. This question paper contains three sections – A, B and C. Each part is compulsory.
 2. Section - A has 20 MCQs, attempt any 16 out of 20.
 3. Section - B has 20 MCQs, attempt any 16 out of 20
 4. Section - C has 10 MCQs, attempt any 8 out of 10.
 5. There is no negative marking.
 6. All questions carry equal marks.
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SECTION - A

(In this section, attempt any 16 questions out of Questions 1 – 20. Each Question is of 1 mark weightage.)

Q1. $\cot(\tan^{-1}a + \cot^{-1}a)$ is equal to:

- (a) not defined (b) $2a$ (c) 0 (d) $\frac{\pi}{2}$

Q2. Relation R in the set N of natural numbers defined as $R = \{(x, y) : y = x + 5 \text{ and } x < 4\}$ is:

- (a) reflexive (b) symmetric (c) transitive (d) None of these

Q3. Two matrices A and B are multiplied to get AB if

- (a) both are rectangular (b) both have same order
(c) no. of columns of A is equal to no. of rows of B (d) no. of rows of A is equal to no. of columns of B

Q4. If matrix $\begin{bmatrix} 0 & 3 & x+y \\ x-y & -2 & 5 \\ 9 & 5 & 3 \end{bmatrix}$ is symmetric matrix, then the values of x and y will be:

- (a) $x=6, y=3$ (b) $x=-6, y=3$ (c) $x=3, y=6$ (d) $x=3, y=-6$

Q5. Let R be the relation in the set N given by $R = \{(a, b) : a = b - 2; b > 6\}$. Choose the correct answer.

- (A) $(2, 4) \in R$ (B) $(3, 8) \in R$ (C) $(6, 8) \in R$ (D) $(8, 7) \in R$

Q6. If $A = \begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix}$, $B = \begin{bmatrix} 3 & 3 & 5 \\ 1 & 0 & 1 \end{bmatrix}$ then order of matrix AB is:

- (a) 2×3 (b) 3×2 (c) 2×2 (d) 3×3

Q7. The value of $\begin{vmatrix} \sin 10^\circ & -\cos 10^\circ \\ \sin 80^\circ & \cos 80^\circ \end{vmatrix}$ is :

- (a) 1 (b) 0 (c) 2 (d) None

Q8. Discontinuity point of the function $f(x)=5x-3$ is

- (a) $x = 3/5$ (b) $x = 5/3$ (c) all points (d) None

Q9. For what value of k is the function $(x) = \begin{cases} \frac{\tan 2x}{x}, & x \neq 0 \\ k, & x = 0 \end{cases}$; at $x = 0$ will be continuous.

- (a) $k = 0$ (b) $k = 1/2$ (c) $k = 2$ (d) None

Q10. Let A be a square matrix of order 3×3 and if $|A| = 5$ then $|A \text{ Adj.} A|$ is equal to:

- (a) 25
(b) 5
(c) 125
(d) 243

Q11. The matrix $\begin{bmatrix} k & 2 \\ 3 & 4 \end{bmatrix}$ is not invertible if k is equal to

- (a) $3/2$
(b) $2/3$
(c) $-3/2$
(d) $-2/3$

Q12. Local maximum value of $h(x) = x + 1$, $x \in (-1, 1)$ is

- (a) 2
(b) 0
(c) -1
(d) Not Defined

Q13. If $A = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$, then A^2 is equal to:

- (a) $\begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$
(b) $\begin{bmatrix} 1 & 0 \\ 1 & 0 \end{bmatrix}$
(c) $\begin{bmatrix} 0 & 1 \\ 0 & 1 \end{bmatrix}$
(d) $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$

Q14. If $A = (a_{ij}) = \begin{bmatrix} 1 & 2 & 5 \\ 1 & -5 & 5 \\ 1 & 4 & -2 \end{bmatrix}$ and $B = (b_{ij}) = \begin{bmatrix} 7 & 10 & -1 \\ -3 & 2 & 4 \\ 9 & 5 & 2 \end{bmatrix}$, then value of $3a_{22} - 5b_{32}$ is:

- (a) -40 (b) -10 (c) 10 (d) None

Q15. If $y = \tan^{-1} \left(\frac{2x}{1-x^2} \right)$ then dy/dx is:

- (a) $\frac{1}{1+x^2}$
(b) $\frac{1}{1-x^2}$
(c) $\frac{2}{1+x^2}$
(d) $\frac{-1}{1+x^2}$

Q16. If $x = a \sec \theta$, $y = b \tan \theta$, then $\frac{d^2y}{dx^2}$ at $\theta = \frac{\pi}{6}$ is:

- (a) $\frac{-3\sqrt{3}b}{a^2}$
(b) $\frac{-2\sqrt{3}b}{a}$
(c) $\frac{-3\sqrt{3}b}{a}$
(d) $\frac{-b}{3\sqrt{3}a^2}$

Q17. Critical points of the function $f(x) = -2x^3 - 9x^2 - 12x + 1$ are

- (a) 1, 2 (b) -1, 2 (c) -1, -2 (d) 1, -2

Q18. The line $y = x + 1$ is a tangent to the curve $y^2 = 4x$ at the point

- (a) (1, 2) (b) (2, 1) (c) (1, -2) (d) (-1, 2)

Q19. The slope of the normal to the curve $y = 2x^2 + 3 \sin x$ at $x = 0$ is:

- (a) 3
(b) 1/3
(c) -3
(d) -1/3

Q20. In linear Programming Problem $Z = \mathbf{ax} + \mathbf{by}$ is known as:

- (e) constraints
(f) Optimal Value
(g) Objective Function
(h) Decision variable

SECTION - B

(In this section, attempt any 16 questions out of Questions 21 – 40. Each Question is of 1 mark weightage.)

Q21. Let $f: \mathbf{R} \rightarrow \mathbf{R}$ be defined as $f(x) = x^4$. Choose the correct answer.

(a) f is one-one and onto (b) f is many-one and onto (c) f is one-one but not onto (d) f is neither one-one nor onto.

Q22. Find x : $2 \sin^{-1}x = \frac{\pi}{3}$

(a) $-\frac{1}{2}$ (b) $\frac{\sqrt{3}}{2}$ (c) $\frac{1}{2}$ (d) None of them

Q23. If $\begin{bmatrix} a+4 & 3b \\ 8 & -6 \end{bmatrix} = \begin{bmatrix} 2a+2 & b+2 \\ 8 & a-8b \end{bmatrix}$, then the value of $2a + b$:

(a) 5 (b) -3 (c) 11 (d) None

Q24. If relation R in the set $A = \{x \in \mathbf{Z} : 0 \leq x \leq 8\}$, given by $R = \{(a, b) : |a - b| \text{ is a multiple of } 4\}$ is an equivalence relation. Then equivalence class of $[2]$ will be:

(a) 2, 6 (b) 0, 4 (c) 4, 8 (d) None of them

Q25. If the given points $(5,5)$, $(k,1)$ and $(10,7)$ lie on a straight line then k will be equal to:

(a) $K=5$
(b) $K=-5$
(c) $K=1/5$
(d) $K=-1/5$

Q26. The function $f: R \rightarrow R$ defined by $f(x) = x - 4$ is:

(a) Bijective (b) Surjective but not injective (c) Injective but not surjective (d) Neither injective nor surjective

Q27. $\tan^{-1}\sqrt{3} - \cot^{-1}(-\sqrt{3})$ is equal to :

(a) $\frac{\pi}{2}$ (b) $-\frac{\pi}{2}$ (c) π (d) 1

Q28. If $A = \begin{bmatrix} 0 & -3 & p \\ 3 & 0 & -4 \\ 1 & q & r \end{bmatrix}$ is a skew sym. matrix then $p + q - r$ will be equal to:

(a) -4 (b) 3 (c) 3 (d) None

Q29. Simplest form of $\tan^{-1}\left(\frac{2\sqrt{x}}{1-x}\right)$ is:

- (a) $\tan^{-1}x$
- (b) $2\tan^{-1}x$
- (c) $2\tan^{-1}\sqrt{x}$
- (d) None

Q30. If $A = \begin{bmatrix} 1 & 2 & -3 \end{bmatrix}$ and $B = \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$ then $(AB)^2$ is equal to:

- (a) 14
- (b) 169
- (c) 16
- (d) None of these

Q31. If A and B are square matrices of the same order and $AB = 3I$ then A^{-1} is equal to :

- (a) $3B$
- (b) $\frac{1}{3}B$
- (c) $3B^{-1}$
- (d) $\frac{1}{3}B^{-1}$

Q32. The region represented by the inequation system $x, y \geq 0, x + y \leq 3$ is

- a) unbounded in first quadrant
- b) unbounded in first and second quadrant
- c) bounded in first quadrant
- d) none of these

Q33. Differentiation of $y = 7^x$ is

- (a) 0
- (b) 7^x
- (c) $\frac{7^x}{\log x}$
- (d) $7^x \log 7$

34. If $y = \log \sqrt{\tan x}$ then value of $\frac{dy}{dx}$ at $x = \frac{\pi}{4}$ is

- (a) ∞
- (b) 0
- (c) 1
- (d) $\frac{1}{2}$

Q35. $f(x) = e^{2x}$ is

- (a) Strictly Increasing on \mathbf{R}
- (b) Strictly Decreasing on \mathbf{R}
- (c) Decreasing on \mathbf{R}
- (d) Neither Increasing nor Decreasing

Q36. Absolute maximum value of $f(x) = x^3, x \in [-2, 2]$ is

- (a) -8
- (b) 0
- (c) 8
- (d) 12

Q37. Local Maximum value of the function $f(x) = \sin(3x) + 7$ is

- (a) 7
- (b) Infinity
- (c) 8
- (d) 10

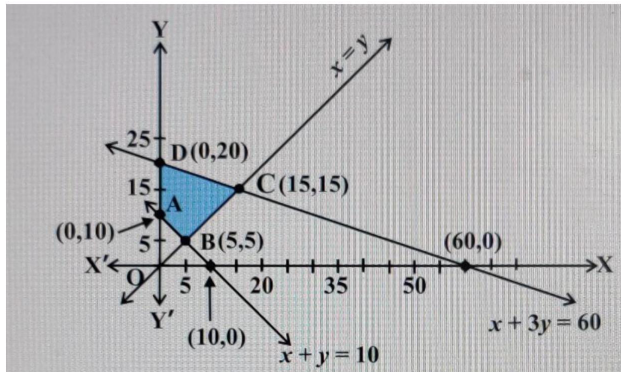
Q38. The points on the curve $\frac{x^2}{9} + \frac{y^2}{16} = 1$ at which the tangents are parallel to y axis are:

- (a) $(0, \pm 4)$
- (b) $(\pm 4, 0)$
- (c) $(\pm 3, 0)$
- (d) $(0, \pm 3)$

Q39. The interval in which $y = x^2 e^{-x}$ is increasing is

- (a) $(-\infty, \infty)$
- (b) $(-2, 0)$
- (c) $(2, \infty)$
- (d) $(0, 2)$

Q40. From the given figure Maximum value of $Z = 3x + 9y$ will be:



- (a) 90
- (b) 280
- (c) 180
- (d) 60

SECTION - C

(In this section, attempt any 8 questions out of Questions 41 – 50. Each Question is of 1 mark weightage.)
(Questions 46-50 are based on a Case Study)

Q41. The variable x and y in a linear programming problem are called:

- (a) Decision variables

- (b) Linear variables
- (c) Optimal variables
- (d) None of these

Q42. If $f(x) = [x]$ is a greatest integer function then it will be continuous if

- (a) $x \in R$
- (b) $x \in [1,5]$
- (c) $x \in (1,2)$
- (d) None

Q43. dy/dx of a function expressed in parametric form $x = \sin t$, $y = \cos 2t$ is

- (a) $4 \sin t$
- (b) $-4 \cos t$
- (c) $\frac{-4}{\operatorname{cosec} t}$
- (d) $4 \operatorname{sect}$

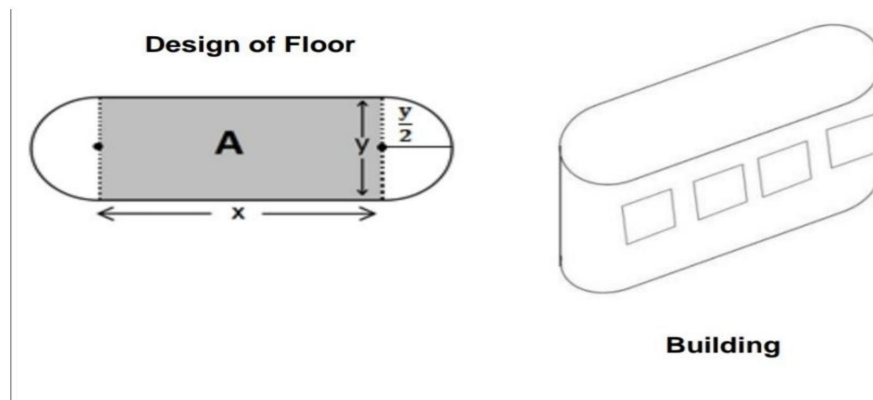
Q44. If corner points of a feasible solution are $(0,8)$, $(4, 10)$, $(6,8)$, $(6,5)$, $(5,0)$, $(0,0)$ and Objective function is $Z = 3x - 4y$ then Minimum of Z occurs at :

- (a) $(0,0)$
- (b) $(0,8)$
- (c) $(5,0)$
- (d) $(4,10)$

Q45. Inverse of matrix $\begin{bmatrix} 2 & -3 \\ 3 & -4 \end{bmatrix}$ is:

- (a) $\begin{bmatrix} -4 & 3 \\ -3 & 2 \end{bmatrix}$
- (b) $\begin{bmatrix} 4 & -3 \\ 3 & -2 \end{bmatrix}$
- (c) $\begin{bmatrix} -2 & 3 \\ -3 & 4 \end{bmatrix}$
- (d) $\begin{bmatrix} 2 & -3 \\ 3 & -4 \end{bmatrix}$

An architect designs a building for a multi-national company. The floor consists of a rectangular region with semicircular ends having a perimeter of 200m as shown below:



Based on the above information answer the following:

Q46. If x and y represents the length and breadth of the rectangular region, then the relation between the variables is

- (a) $x + \pi y = 100$
- (b) $2x + \pi y = 200$
- (c) $\pi x + y = 50$
- (d) $x + y = 100$

Q47. The area of the rectangular region A expressed as a function of x is

- (a) $\frac{2}{\pi} (100x - x^2)$
- (b) $\frac{1}{\pi} (100x - x^2)$
- (c) $\frac{x}{\pi} (100 - x)$
- (d) $\pi y^2 + \frac{2}{\pi} (100x - x^2)$

Q48. The maximum value of area A is

- (a) $\frac{\pi}{3200} m^2$
- (b) $\frac{3200}{\pi} m^2$
- (c) $\frac{5000}{\pi} m^2$
- (d) $\frac{1000}{\pi} m^2$

Q49. The CEO of the multi-national company is interested in maximizing the area of the whole floor including the semi-circular ends. For this to happen the value of x should be :

- a) 0 m
- b) 30 m
- c) 50 m
- d) 80

Q50. The extra area generated if the area of the whole floor is maximized is :

- a) $\frac{3000}{\pi} m^2$
- b) $\frac{5000}{\pi} m^2$
- c) $\frac{7000}{\pi} m^2$
- d) No change Both areas are equal
